## GCSE (9-1) Mathematics J560/04 Paper 4 (Higher Tier) Sample Question Paper

## Date - Morning/Afternoon

Time allowed: 1 hour 30 minutes

## You may use:

- A scientific or graphical calculator
- Geometrical instruments
- Tracing paper



## INSTRUCTIONS

- Use black ink. You may use an HB pencil for graphs and diagrams.
- Complete the boxes above with your name, centre number and candidate number.
- Answer all the questions.
- Read each question carefully before you start to write your answer.
- Where appropriate, your answers should be supported with working. Marks may be given for a correct method even if the answer is incorrect.
- Write your answer to each question in the space provided.
- Additional paper may be used if required but you must clearly show your candidate number, centre number and question number(s).
- Do not write in the bar codes.


## INFORMATION

- The total mark for this paper is 100.
- The marks for each question are shown in brackets [ ].
- Use the $\pi$ button on your calculator or take $\pi$ to be 3.142 unless the question says otherwise.
- This document consists of 20 pages.

Answer all the questions

118 rice cakes weigh a total of 130 g . There are 329 calories in 100 g of rice cakes.

How many calories are there in one rice cake?
$\qquad$ calories [3]

2 A circular table top has radius 70 cm .
(a) Calculate the area of the table top in $\mathrm{cm}^{2}$, giving your answer as a multiple of $\pi$.
(a)
$\mathrm{cm}^{2}$ [2]
(b) The volume of the table top is $17150 \pi \mathrm{~cm}^{3}$.

Calculate the thickness of the table top.
(b)
cm [2]

3 The value of a car $£ V$ is given by

$$
V=20000 \times 0.9^{t}
$$

where $t$ is the age of the car in complete years.
(a) Write down the value of $V$ when $t=0$.
(a) $£$
[1]
(b) What is the value of $V$ when $t=3$ ?
(b) $£$
(c) After how many complete years will the car's value drop below $£ 10000$ ?
(c)

4 (a) (i) Sketch a graph on the axes below that shows that $y$ is directly proportional to $x$.

(ii) Sketch a graph on the axes below that shows $y=x^{3}$.

(b) It is possible to draw many rectangles that have area $24 \mathrm{~cm}^{2}$. Here are two of them.

(i) Plot the dimensions of these two rectangles on the grid below.
(ii) Complete the graph to show the relationship between length and width for rectangles with area $24 \mathrm{~cm}^{2}$.


5 Kieran, Jermaine and Chris play football.

- Kieran has scored 8 more goals than Chris.
- Jermaine has scored 5 more goals than Kieran.
- Altogether they have scored 72 goals.

How many goals did they each score?

Kieran
Jermaine $\qquad$
Chris $\qquad$

6 Peter makes a large amount of pink paint by mixing red and white paint in the ratio $2: 3$.

Red paint costs $£ 80$ per 10 litres.
White paint costs $£ 5$ per 10 litres.
Peter sells his pink paint in 10 -litre tins for $£ 60$ per tin.

Calculate how much profit he makes for each tin he sells.

7 Dan believes he knows what his brother Ethan is thinking.
He carries out an experiment to test this.
Dan and Ethan sit back-to-back.
Ethan rolls an ordinary fair dice.
Ethan then thinks about the number on the dice while Dan tries to predict this number.
(a) In 300 attempts, how many correct predictions would you expect Dan to make if he was just guessing?
(a)
(b) The results of the first 15 attempts are shown in the table.

| Ethan's number | 2 | 6 | 5 | 3 | 2 | 1 | 5 | 1 | 3 | 4 | 4 | 6 | 1 | 6 | 5 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Dan's prediction | 2 | 4 | 3 | 1 | 2 | 6 | 1 | 6 | 4 | 3 | 2 | 6 | 5 | 2 | 3 |
| Matching pair | $\checkmark$ |  |  |  | $\checkmark$ |  |  |  |  |  |  | $\checkmark$ |  |  |  |

Estimate the probability of getting a matching pair using the results of
(i) the first five attempts,
(b)(i)
(ii) all 15 attempts.
(ii)
(c) Use answers from (a) and (b) to comment on Dan's belief that he knows what Ethan is thinking.
$\qquad$
$\qquad$
$\qquad$

8 (a) A function is represented by the following function machine.

(i) A number is input into the machine.

The output is used as a new input.
The second output is 11 .
Work out the number that was the first input.

> (a)(i)
[2]
(ii) A number is input into the machine.

The output given is the same number.
Work out the number.
(ii)
(b) Another function machine is shown below.


If the Input is 3 , the Output is 5 .
If the Input is 7 , the Output is 25 .
Use this information to fill in the two boxes.

9 (a) Anna estimates the height of a tree.


Anna holds a ruler vertically so the height of the tree is exactly covered by the ruler. She is 20 metres from the tree.
The ruler is 30 cm long.
The horizontal distance from her eyes to the ruler is 60 cm .
Calculate an estimate of the height of the tree.
(a) $\qquad$
(b) Give two reasons why this method may not be suitable to estimate the height of a very tall building.

10 ABCD is a parallelogram.


Prove that triangle ABD is congruent to triangle CDB.

11 (a) Give one reason why 0 is an even number.
$\qquad$
(b) The lengths of the sides of a right-angled triangle are all integers.

Prove that if the lengths of the two shortest sides are even, then the length of the third side must also be even.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

12 (a) Without using a calculator, show that $\sqrt{20}=2 \sqrt{5}$.
(b) The point A is shown on the unit grid below.

The point $B$ is $2 \sqrt{5}$ units from $A$ and lies on the intersection of two grid lines.
Mark one possible position for $B$.


13 The volume of Earth is $1.08 \times 10^{12} \mathrm{~km}^{3}$.
The volume of Jupiter is $1.43 \times 10^{15} \mathrm{~km}^{3}$.
How many times larger is the radius of Jupiter than the radius of Earth?
Assume that Jupiter and Earth are both spheres.
[The volume $v$ of a sphere with radius $r$ is $v=\frac{4}{3} \pi r^{3}$.]

14 The table shows the marks gained by 150 students taking an examination.

| Mark $(m)$ | $0<m \leqslant 10$ | $10<m \leqslant 20$ | $20<m \leqslant 30$ | $30<m \leqslant 40$ | $40<m \leqslant 50$ | $50<m \leqslant 60$ | $60<m \leqslant 70$ | $70<m \leqslant 80$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 9 | 14 | 26 | 27 | 25 | 22 | 17 | 10 |

(a) (i) Construct a cumulative frequency table.

| Mark $(m)$ | $m \leqslant 10$ | $m \leqslant 20$ | $m \leqslant 30$ | $m \leqslant 40$ | $m \leqslant 50$ | $m \leqslant 60$ | $m \leqslant 70$ | $m \leqslant 80$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cumulative <br> Frequency | 9 |  |  |  |  |  |  | 150 |

(ii) Draw the cumulative frequency graph on the grid below.

(b) Students are to be awarded Gold, Silver, Bronze or Fail.

The students' teacher wishes to award the top 10\% of students Gold, the next 60\% Silver and the next $20 \%$ Bronze.

Use your graph to estimate the lowest mark that Silver will be awarded for.
(b)
(c) Explain why the teacher's method will not necessarily award Gold to exactly $10 \%$ of the students.
$\qquad$

15 At a constant temperature, the volume of a gas $V$ is inversely proportional to its pressure $p$. By what percentage will the pressure of a gas change if its volume increases by $25 \%$ ?
$16 \mathrm{~A}, \mathrm{~B}, \mathrm{C}$ and D are points on the circumference of a circle, centre O . $A C$ is a diameter of the circle.
Angle ABD $=58^{\circ}$.
Angle CDB $=22^{\circ}$.


## Not to scale

Work out the sizes of angle ACD and ACB, giving reasons for your answers.
(a) Angle ACD = $\qquad$ .
$\qquad$
(b) Angle ACB = $\qquad$ .${ }^{\circ}$
$\qquad$
$\qquad$
$\qquad$

17 A restaurant menu has 8 starters, 12 mains and 6 desserts.
A customer can choose from the following meals

- a starter and a main,
- a main and a dessert,
- a starter, a main and a dessert.

Show that there are 744 different ways of choosing a meal at this restaurant.

18 Four pencils are held together with a band.
The figure below shows the bottom end of the pencils and the band.


Each of the pencils has diameter 9 mm .
Find the length of the band in this position.

19 A sequence is defined by the term-to-term rule $u_{n+1}=u_{n}^{2}-8 u_{n}+17$.
(a) Given that $u_{1}=4$, find $u_{2}$ and $u_{3}$.
(a)
[2]
(b) Given instead that $u_{1}=2$, find $u_{2}, u_{3}$ and $u_{100}$.
(b)

20 (a) Express as a single fraction.

$$
\frac{m+1}{n+1}-\frac{m}{n}
$$

Simplify your answer.
(a)
[2]
(b) Using your answer to part (a), prove that if $m$ and $n$ are positive integers and $m<n$, then

$$
\frac{m+1}{n+1}-\frac{m}{n}>0
$$

[^0]Date - Morning/Afternoon
GCSE (9-1) Mathematics
J560/04 Paper 4 (Higher Tier)

SAMPLE MARK SCHEME

## MAXIMUM MARK <br> 100



## Subject-Specific Marking Instructions

1. M marks are for using a correct method and are not lost for purely numerical errors.

A marks are for an accurate answer and depend on preceding M (method) marks. Therefore M0 A1 cannot be awarded.
B marks are independent of $\mathbf{M}$ (method) marks and are for a correct final answer, a partially correct answer, or a correct intermediate stage.
SC marks are for special cases that are worthy of some credit.
2. Unless the answer and marks columns of the mark scheme specify $\mathbf{M}$ and $\mathbf{A}$ marks etc, or the mark scheme is 'banded', then if the correct answer is clearly given and is not from wrong working full marks should be awarded.

Do not award the marks if the answer was obtained from an incorrect method, ie incorrect working is seen and the correct answer clearly follows from it.
3. Where follow through (FT) is indicated in the mark scheme, marks can be awarded where the candidate's work follows correctly from a previous answer whether or not it was correct.

Figures or expressions that are being followed through are sometimes encompassed by single quotation marks after the word their for clarity, e.g. FT $180 \times$ (their ' 37 ' +16 ), or $\mathrm{FT} 300-\sqrt{ }$ (their ' $5^{2}+7^{2}$ ). Answers to part questions which are being followed through are indicated by e.g. FT $3 \times$ their (a).

For questions with FT available you must ensure that you refer back to the relevant previous answer. You may find it easier to mark these questions candidate by candidate rather than question by question.
4. Where dependent (dep) marks are indicated in the mark scheme, you must check that the candidate has met all the criteria specified for the mark to be awarded.
5. The following abbreviations are commonly found in GCSE Mathematics mark schemes.

- figs 237, for example, means any answer with only these digits. You should ignore leading or trailing zeros and any decimal point e.g. $237000,2.37,2.370,0.00237$ would be acceptable but 23070 or 2374 would not.
- isw means ignore subsequent working after correct answer obtained and applies as a default.
- nfww means not from wrong working.
- oe means or equivalent.
- rot means rounded or truncated.
- seen means that you should award the mark if that number/expression is seen anywhere in the answer space, including the answer line, even if it is not in the method leading to the final answer.
- soi means seen or implied.

6. In questions with no final answer line, make no deductions for wrong work after an acceptable answer (ie isw) unless the mark scheme says otherwise, indicated by the instruction 'mark final answer'.
7. In questions with a final answer line following working space:
(i) If the correct answer is seen in the body of working and the answer given on the answer line is a clear transcription error allow full marks unless the mark scheme says 'mark final answer'. Place the annotation $\checkmark$ next to the correct answer.
(ii) If the correct answer is seen in the body of working but the answer line is blank, allow full marks. Place the annotation $\checkmark$ next to the correct answer.
(iii) If the correct answer is seen in the body of working but a completely different answer is seen on the answer line, then accuracy marks for the answer are lost. Method marks could still be awarded. Use the M0, M1, M2 annotations as appropriate and place the annotation $\times$ next to the wrong answer.
8. In questions with a final answer line:
(i) If one answer is provided on the answer line, mark the method that leads to that answer.
(ii) If more than one answer is provided on the answer line and there is a single method provided, award method marks only.
(iii) If more than one answer is provided on the answer line and there is more than one method provided, award zero marks for the question unless the candidate has clearly indicated which method is to be marked.
9. In questions with no final answer line:
(i) If a single response is provided, mark as usual.
(ii) If more than one response is provided, award zero marks for the question unless the candidate has clearly indicated which response is to be marked.
10. When the data of a question is consistently misread in such a way as not to alter the nature or difficulty of the question, please follow the candidate's work and allow follow through for $\mathbf{A}$ and $\mathbf{B}$ marks. Deduct 1 mark from any $\mathbf{A}$ or $\mathbf{B}$ marks earned and record this by using the MR annotation. $\mathbf{M}$ marks are not deducted for misreads.
11. Unless the question asks for an answer to a specific degree of accuracy, always mark at the greatest number of significant figures even if this is rounded or truncated on the answer line. For example, an answer in the mark scheme is 15.75 , which is seen in the working. The candidate then rounds or truncates this to $15.8,15$ or 16 on the answer line. Allow full marks for the 15.75 .
12. Ranges of answers given in the mark scheme are always inclusive.
13. For methods not provided for in the mark scheme give as far as possible equivalent marks for equivalent work. If in doubt, consult your Team Leader.
14. Anything in the mark scheme which is in square brackets [...] is not required for the mark to be earned, but if present it must be correct.

| Question |  | Answer | Marks | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  | $23.6-23.8$ <br> Accept 24 provided full method shown | $\begin{gathered} \hline 3 \\ \text { 1AO1.3b } \\ 2 \text { AO3.1c } \end{gathered}$ | M2 for $\frac{329 \times 130}{18 \times 100}$ <br> Or <br> M1 for any two of $\frac{329}{100}$ or $\frac{130}{100}$ or $\frac{329}{18}$ or $329 \times 130$ | May be done in stages |
| 2 | (a) | $4900 \pi$ | $\begin{gathered} 2 \\ 1 \text { A01.2 } \\ 1 \text { AO1.3a } \end{gathered}$ | M1 for $\pi \times 70^{2}$ may be implied by 15393.8... |  |
|  | (b) | 3.5 | $\begin{gathered} 2 \\ 2 \mathrm{AOO} .3 \mathrm{a} \end{gathered}$ | $\text { M1 for } \frac{17150 \pi}{\text { their }{ }^{\prime} 4900 \pi \pi^{\prime}}$ | FT from (a), provided (a) is a multiple of $\pi$ |
| 3 | (a) | $£ 20000$ | $\begin{gathered} \hline 1 \\ 1 \text { AO1.3a } \end{gathered}$ |  |  |
|  | (b) | $£ 14580$ or £14 600 | $\begin{gathered} 2 \\ 2 \mathrm{AO} 1.3 \mathrm{a} \end{gathered}$ | M1 for $20000 \times 0.9^{3}$ |  |
|  | (c) | 7 years | $\begin{gathered} 2 \\ 1 \text { AO1.3a } \\ 1 \text { AOB.1c } \end{gathered}$ | M1 for 2 trials shown |  |


| Question |  |  | Answer <br> Any straight line through the origin e.g. | Marks <br> 2 <br> 1 A01.1 <br> 1 AO2.3b | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 4 | (a) | (i) |  |  | B1 for a straight line |  |
|  |  | (ii) |  | 2 1 AO1.1 1 AO2.3b | B1 for a cubic with two turning points |  |
|  | (b) | (i) | At least one point plotted correctly | $\begin{gathered} 1 \\ 1 \text { AO2.3b } \end{gathered}$ |  |  |



| Question |  |  | Answer | Marks | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 6 |  |  | £25 | $\begin{gathered} 5 \\ 2 \text { AO1.3b } \\ 3 \text { AO3.1d } \end{gathered}$ | M1 for $10 \times \frac{2}{5}=4$ litres red or $10 \times \frac{3}{5}=6$ litres white <br> M1 for red costs $£ 8$ per litre or white costs $£ 0.50$ per litre M1 for cost of one 10-litre can is their ' 4 ' $\times$ their ' 8 ' + their ' 6 ' $\times$ their ' 0.5 ' M1 for 60 - their ' 35 ' | Alternative method: <br> M1 for 2: 3 = 20 litres red : 30 litres white <br> M1 for $2 \times £ 80+3 \times £ 5=£ 175$ <br> M1 for $\frac{\text { their '175' }}{5}=35$ <br> M1 for 60 - their ' 35 ' |
| 7 | (a) |  | 50 | $\begin{gathered} 2 \\ 2 \text { A01.3a } \end{gathered}$ | $\text { B1 for } \frac{1}{6}$ |  |
|  | (b) | (i) | $\frac{2}{5} \text { oe }$ | $\begin{gathered} 1 \\ 1 \text { AO2.1b } \end{gathered}$ |  |  |
|  |  | (ii) | $\frac{1}{5} \text { oe }$ | $\begin{gathered} 1 \\ 1 \text { AO2.1b } \end{gathered}$ |  |  |
|  | (c) |  | No evidence that Dan knows what Ethan is thinking as over the 15 trials the relative frequency of $\frac{1}{5}$ is very close to the theoretical probability of $\frac{1}{6}$ |  | M1 for reason not including reference to $\frac{1}{5}$ relative frequency or $\frac{1}{6}$ theoretical probability <br> FT their (a) and (b) |  |
| 8 | (a) | (i) | -1 |  | M1 for use of -5 and $\div 2$ soi Or <br> M1 for answer 3 |  |


| Question |  |  | Answer | Marks | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | (ii) | -5 |  | M1 for $2 x+5$ <br> M1 for $x=$ their ' $2 x+5$ ' and solve |  |
|  | (b) |  | 5, 10 |  | M1 for $3 a+b=5$ and $7 a+b=25$ M1 for attempt to solve <br> Or <br> M1 input increases by 4; output increases by 20 <br> M1 so one box must have $\times 5$ for the arithmetic sequence | Condone $\frac{x^{2}+1}{2}$ across the two boxes for 3 marks |
| 9 | (a) |  | 10 metres |  | M1 for correct ratio $\frac{\text { height }}{20}=\frac{30}{60}$ oe M1 rearrange <br> Or <br> M1 for scale factor 0.5 <br> M1 for $20 \times 0.5$ |  |
|  | (b) |  | 2 valid reasons, <br> e.g. She would have to be very far from the building. <br> The estimate is likely to be inaccurate due to the scale factors at the distances involved. | $\begin{gathered} 2 \\ 2 \text { AO3.4a } \end{gathered}$ |  |  |


| Question |  | Answer | Marks | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 10 |  | e.g. <br> $B D$ is common <br> ABD = BDC (alternate angles) <br> $A B=C D$ (parallelogram) <br> So triangles $A B D$ and CBD are congruent by SAS | $\begin{gathered} 3 \\ 1 \text { AO1.1 } \\ 2 \text { AO2.4b } \end{gathered}$ | B2 for two facts with conclusion or <br> B2 for three facts with conclusion missing or unclear or <br> B1 for one correct fact | Each fact must be backed up with a reason |
| 11 | (a) | Any correct reason | $\begin{gathered} 1 \\ 1 \text { AO2.4a } \end{gathered}$ |  | Exemplar responses: <br> -1 and 1 both odd and either side of 0 <br> Or can be divided by 2 exactly <br> Or numbers that end in 0 are even <br> Or zero remainder when divided by 2 <br> Or next number in pattern of even numbers <br> 8642 <br> Or added to an even number it gives even answer and added to odd number gives odd answer |
|  | (b) | e.g. $\begin{aligned} & a^{2}+b^{2}=c^{2} \\ & a=2 x \text { and } b=2 y \text { implies } c^{2}=4 x^{2}+4 y^{2} \end{aligned}$ <br> So $c$ is even | $\begin{gathered} \hline 3 \\ 1 \text { AO2.1a } \\ 1 \text { AO2.4b } \\ 1 \text { AO3.2 } \end{gathered}$ | B1 for use of Pythagoras' theorem M1 for even $\times$ even $=$ even soi |  |


| Question |  | Answer | Marks | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 12 | (a) | $\begin{aligned} & \sqrt{20}=\sqrt{4 \times 5} \\ & =\sqrt{4} \times \sqrt{5} \\ & =2 \sqrt{5} \end{aligned}$ | $\begin{gathered} 2 \\ 2 \text { A01.3a } \end{gathered}$ | M1 for $\sqrt{4} \times \sqrt{5}$ |  |
|  | (b) | Either <br> point which is 4 across and 2 up from $A$ or 2 across and 4 up | 3 1 AO2.3b 1 AO3.1a 1 AO3.2 | B1 for $a^{2}+b^{2}=20$ <br> B1 for 4 and 16 (or 2 and 4) seen <br> If zero scored SC1 for correctly marking the position of their $a$ and $b$ | Condone both correct points marked |
| 13 |  | 11 or better | $\begin{gathered} \hline 4 \\ 2 \text { AO1.3b } \\ 1 \text { AOB.1b } \\ 1 \text { AO3.2 } \end{gathered}$ | M1 for $r=\sqrt[3]{\frac{3 v}{4 \pi}}$ soi <br> A1 for $r$ (Earth) $=6365 \mathrm{~km}$ <br> or $r$ (Jupiter) $=69890 \mathrm{~km}$ <br> M1 for $\frac{\text { their '69890' }}{\text { their '6365' }}$ | Alternate method: <br> M1 for $\frac{1.43 \times 10^{15}}{1.08 \times 10^{12}}$ <br> A1 for 1324[.074...] <br> M1 for $\sqrt[3]{1324}$ |


| Question |  |  |  Answer <br> Table:  <br> 923  | Marks <br> 2 <br> 2 A01.3a | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 14 | (a) | (i) |  |  | M1 for attempt to accumulate the values |  |
|  |  | (ii) |  | $\begin{gathered} \hline 4 \\ 1 \text { AO1.3b } \\ 3 \text { AOO2.3b } \end{gathered}$ | B1 for labelling axes <br> B1 for correct curve through points B1 for at least six points correctly plotted |  |
|  | (b) |  | 28-32 | $\begin{gathered} \hline 3 \\ 2 \text { A02.1b } \\ 1 \text { A02.3a } \end{gathered}$ | M1 for 45 or 105 seen <br> A1 for corresponding answer <br> FT their graph |  |
|  | (c) |  | The boundaries are set from approximations based on grouped data, not the actual scores obtained by the students | $\begin{gathered} 1 \\ 1 \text { A02.5b } \end{gathered}$ |  |  |
| 15 |  |  | 20 [decrease](%25) | 4 <br> 1 AO1.1 <br> 1 AO1.3b <br> 2 AO3.1d | M1 for $p V=$ constant oe <br> $\mathbf{M 1}$ for $p_{\text {initial }} V_{\text {initial }}=p_{\text {after }} V_{\text {after }}$ oe <br> $\mathbf{M 1}$ for $1 \times 1=p_{\text {after }} \times 1.25$ oe |  |


| Question |  | Answer | Marks | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 16 | (a) | $58^{\circ}$ <br> Subtended on same arc oe | $\begin{gathered} 2 \\ 1 \text { AOO.1a } \\ 1 \text { AO2.4b } \end{gathered}$ | B1 for angle |  |
|  | (b) | $68^{\circ}$ <br> e.g. <br> angle DBC is $32^{\circ}$ because the angle in a semicircle is a right angle oe so angle ACB is $68^{\circ}$ because angles in a triangle sum to $180^{\circ}$ oe | $\begin{gathered} \hline 3 \\ 2 \mathrm{AO} .1 \mathrm{a} \\ 1 \mathrm{AOO} .4 \mathrm{~b} \end{gathered}$ | B1 for using the angle in a semicircle is a right angle <br> B1 for using angles in a triangle sum to $180^{\circ}$ |  |
| 17 |  | Starter and main $8 \times 12$ <br> Main and dessert $12 \times 6$ <br> Three courses $8 \times 12 \times 6$ $96+72+576=744$ | $\begin{gathered} \hline 3 \\ 1 \text { AO1.3b } \\ 1 \text { AO2.1a } \\ 1 \text { AO2.2 } \end{gathered}$ | M1 for one correct product M1 for summing their three products |  |
| 18 |  | 64.3 or $9 \pi+36$ oe | $\begin{gathered} \hline 4 \\ 2 \text { AO1.3b } \\ 2 \text { AO3.1d } \end{gathered}$ | M1 for $\frac{9 \pi}{4}$ soi <br> A1 for $9 \pi$ or 28.2[7...] <br> M1 for their ' $9 \pi$ ' +36 |  |
| 19 | (a) | 1 nfww 10 nfww | $\begin{gathered} \hline 2 \\ 1 \text { AO1.2 } \\ 1 \text { AO1.3a } \end{gathered}$ | B1 for each | FT their ' $u_{2}$ ' for $u_{3}$ |
|  | (b) | 5 nfww <br> 2 nfww <br> 5 nfww | 13 1 AO1.2 1 A01.3a 1 AO2.1a | B1 for each | FT their ' $u_{2}$ ' for $u_{3}$ |


| Question |  | Answer | Marks | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 20 | (a) | $\frac{n-m}{n(n+1)}$ | $\begin{gathered} 2 \\ 2 \mathrm{AO} 1.3 \mathrm{~b} \end{gathered}$ | M1 for $\frac{n(m+1)-m(n+1)}{n(n+1)}$ |  |
|  | (b) | $\begin{aligned} & m<n \Rightarrow n-m>0 \\ & \Rightarrow \frac{n-m}{n(n+1)}>0 \\ & \Rightarrow \frac{m+1}{n+1}-\frac{m}{n}>0 \end{aligned}$ | $\begin{gathered} 2 \\ 2 \text { AO2.4b } \end{gathered}$ | $\mathbf{M 1}$ for their $\frac{n-m}{n(n+1)}>0$ |  |

Assessment Objectives (AO) Grid

| Question | A01 | AO2 | AO3 | Total |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 1 |  | 2 | 3 |
| 2(a) | 2 |  |  | 2 |
| 2(b) | 2 |  |  | 2 |
| 3(a) | 1 |  |  | 1 |
| 3(b) | 2 |  |  | 2 |
| 3(c) | 1 |  | 1 | 2 |
| 4(a)(i) | 1 | 1 |  | 2 |
| 4(a)(ii) | 1 | 1 |  | 2 |
| 4(b)(i) |  | 1 |  | 1 |
| 4(b)(ii) |  | 1 | 2 | 3 |
| 5 | 2 |  | 3 | 5 |
| 6 | 2 |  | 3 | 5 |
| 7(a) | 2 |  |  | 2 |
| 7(b)(i) |  | 1 |  | 1 |
| 7(b)(ii) |  | 1 |  | 1 |
| 7(c) |  | 1 | 1 | 2 |
| 8(a)(i) | 1 |  | 1 | 2 |
| 8(a)(ii) | 1 |  | 2 | 3 |
| 8(b) | 1 |  | 2 | 3 |
| 9(a) | 1 |  | 2 | 3 |
| 9(b) |  |  | 2 | 2 |
| 10 | 1 | 2 |  | 3 |
| 11(a) |  | 1 |  | 1 |
| 11(b) |  | 2 | 1 | 3 |
| 12(a) | 2 |  |  | 2 |
| 12(b) |  | 1 | 2 | 3 |
| 13 | 2 |  | 2 | 4 |
| 14(a)(i) | 2 |  |  | 2 |
| 14(a)(ii) | 1 | 3 |  | 4 |
| 14(b) |  | 3 |  | 3 |
| 14(c) |  | 1 |  | 1 |
| 15 | 2 |  | 2 | 4 |
| 16(a) |  | 2 |  | 2 |
| 16(b) |  | 3 |  | 3 |
| 17 | 1 | 2 |  | 3 |
| 18 | 2 |  | 2 | 4 |
| 19(a) | 2 |  |  | 2 |
| 19(b) | 2 | 1 |  | 3 |
| 20(a) | 2 |  |  | 2 |
| 20(b) |  | 2 |  | 2 |
| Totals | 40 | 30 | 30 | 100 |

## GCSE (9-1) Mathematics J560/05 Paper 5 (Higher Tier) Sample Question Paper

## Date - Morning/Afternoon

Time allowed: 1 hour 30 minutes

You may use:

- Geometrical instruments
- Tracing paper

Do not use:

- A calculator



## INSTRUCTIONS

- Use black ink. You may use an HB pencil for graphs and diagrams.
- Complete the boxes above with your name, centre number and candidate number.
- Answer all the questions.
- Read each question carefully before you start to write your answer.
- Where appropriate, your answers should be supported with working. Marks may be given for a correct method even if the answer is incorrect.
- Write your answer to each question in the space provided.
- Additional paper may be used if required but you must clearly show your candidate number, centre number and question number(s).
- Do not write in the bar codes.


## INFORMATION

- The total mark for this paper is 100.
- The marks for each question are shown in brackets [ ].
- This document consists of $\mathbf{2 0}$ pages.

Answer all the questions

1 (a) Here is a coordinate grid.


Shape $S$ is translated to Shape T using vector $\binom{p}{q}$.
Write down the values of $p$ and $q$.
(a) $p=$
$q=$
(b) Vectors $\mathbf{a}, \mathbf{b}, \mathbf{c}, \mathbf{d}$ and $\mathbf{e}$ are drawn on an isometric grid.


Write each of the vectors $\mathbf{c}, \mathbf{d}$ and $\mathbf{e}$ in terms of $\mathbf{a}$ and/or $\mathbf{b}$.

$$
\begin{aligned}
& \mathbf{c}= \\
& \mathbf{d}= \\
& \mathbf{e}=
\end{aligned}
$$

2 Sam and two friends put letters in envelopes on Monday.
The three of them take two hours to put 600 letters in envelopes.
(a) On Tuesday Sam has three friends helping.

Working at the same rate, how many letters should the four of them be able to put in envelopes in two hours?
(a)
(b) Working at the same rate, how much longer would it take four people to put 1000 letters in envelopes than it would take five people?

## (b)

(c) Sam says

It took two hours for three people to put 600 letters in envelopes.
If I assume they work all day, then in one day three people will put 7200 letters in envelopes because $600 \times 12=7200$.

Why is Sam's assumption not reasonable?
What effect has Sam's assumption had on her answer?

3 Abi, Ben and Carl each drop a number of identical drawing pins, and count how many land with the pin upwards. The table shows some of their results.

|  | Number of pins <br> dropped | Number landing <br> 'pin up' |
| :--- | :---: | :---: |
| Abi | 10 | 4 |
| Ben | 30 | 9 |
| Carl | 100 | 35 |

(a) Abi says

As a drawing pin can only land with its pin up or with its pin down, the probability of a drawing pin landing 'pin up' is $\frac{1}{2}$.

Criticise her statement.
$\qquad$
$\qquad$
(b) Carl's results give the best estimate of the probability of a drawing pin landing 'pin up'. Explain why.
$\qquad$
$\qquad$
(c) Two pins are dropped.

Estimate the probability that both pins land 'pin up'.
(c)

John is going to make chocolate squares to sell.

There are just three ingredients, chocolate, peanut butter and crisped rice, mixed in the ratio 4:2:3 respectively.
(a) How much of each ingredient will he need to make 900 g of mixture?
(a) chocolate
$\qquad$ crisped riceg
(b) A bar of chocolate weighs 200 g and costs $£ 2.50$.

A jar of peanut butter contains 250 g and costs $£ 1.70$.
A packet of crisped rice contains 300 g and costs $£ 2.00$.

John makes 4.5 kg of mixture, from which he can cut 100 chocolate squares.
He charges 60p for each square and sells all 100 squares.

How much profit does he make?
(b) $£$

5 The perimeter of the triangle is the same length as the perimeter of the square.


Find an expression for the length of one side of the square in terms of $a$.
Give your answer in its simplest form.

6 A bag contains only red and blue marbles.
Yasmine takes one marble at random from the bag.
The probability that she takes a red marble is $\frac{1}{5}$.
Yasmine returns the marble to the bag and adds five more red marbles to the bag.
The probability that she takes one red marble at random is now $\frac{1}{3}$.
How many marbles of each colour were originally in the bag?
red marbles
blue marbles

7 The lengths of the sides of two squares are integers, when measured in cm . The difference between the areas of the two squares is $36 \mathrm{~cm}^{2}$.

Find the lengths of the sides of the two squares.
cm
cm

8 Safety rules on a campsite require Sarah to set up her barbecue at least 4 m from her tent.
She decides to measure this distance using her stride length.
Sarah knows that her stride length is 0.8 m , rounded to the nearest 0.1 m .

Find the minimum number of strides Sarah will need to take to guarantee that her barbecue is a safe distance from her tent.

9 A sculptor needs to lift a piece of marble.
It is a cuboid with dimensions 1 m by 0.5 m by 0.2 m .
Marble has a density of $2.7 \mathrm{~g} / \mathrm{cm}^{3}$.
The sculptor's lifting gear can lift a maximum load of 300 kg .

Can the lifting gear be used to lift the marble? Justify your decision.

10 Here is a picture of three towers.
Not all the cubes can be seen in the towers.


Tower 1


Tower 2


Tower 3

Edith uses 1 cube to build tower 1 .
Edith uses 6 cubes to build tower 2 . There are 5 cubes on the bottom layer.
(a) Write down the total number of cubes in tower 3.
(a)
(b) Draw a plan view of the arrangement of cubes Edith will use for the bottom layer of tower 4 .

(c) Continue this sequence to show the number of cubes used for the bottom layer of each tower.

| Tower 1 | Tower 2 | Tower 3 | Tower 4 |
| :---: | :---: | :---: | :---: |
| 1 | 5 | ............ |  |

(d) Find an expression for the number of cubes used in the bottom layer of tower $n$.
(d)

11 A toy car is placed on the floor of a sports hall.

It moves in a straight line starting from rest.
It travels with constant acceleration for 4 seconds reaching a velocity of $5 \mathrm{~m} / \mathrm{s}$.
It then slows down with constant deceleration of $1 \mathrm{~m} / \mathrm{s}^{2}$ for 2 seconds.
It then hits a wall and stops.
(a) Draw a velocity-time graph for the toy car.

(b) Work out the total distance travelled by the toy car.
(b)

12 Three identical small circles are drawn inside one large circle, as shown in the diagram. The centres of the small circles lie on the diameter of the large circle.


Find the fraction of the large circle that is shaded.

13 One day a museum monitored the time spent by visitors at six exhibitions. The visitor times are summarised in the box plots below.

Visitor Times

(a) Work out the range in visitor times at the Fantastic Frogs exhibition.
(a)
(b) At which exhibition were visitor times the most consistent?

Give a reason for your answer.
$\qquad$
$\qquad$
$\qquad$
(c) Give one similarity and one difference between the distributions of the visitor times for Origins of the Steam Engine and The Philippine Revolution.

Similarity
$\qquad$
Difference
(d) Is it possible to work out from the box plots which exhibition had the most visitors? Justify your answer.
$\qquad$
$\qquad$
$\qquad$
$\qquad$

14 Show that line $3 y=4 x-14$ is perpendicular to line $4 y=-3 x+48$.

15 (a) Write this list of numbers in order, smallest first.

$$
\sqrt{35}, \frac{20}{3}, \quad 2.5^{2}, \quad 6.83
$$

(a) $\qquad$
(b) Write $(1+\sqrt{3})^{2}$ in the form $a+b \sqrt{3}$.
(b)

16 Bethany says that $(2 x)^{2}$ is always greater than or equal to $2 x$.
Decide whether she is correct or not.
Show your working to justify your decision.

17 (a) Write down the exact value of $\tan 60^{\circ}$.
(a)
[1]
(b) Find the exact area of this triangle.

(b)
$\mathrm{cm}^{2}$ [4]
$18 \mathrm{P}, \mathrm{Q}, \mathrm{R}$ and S are the midpoints of $\mathrm{OX}, \mathrm{XY}, \mathrm{YZ}$ and OZ respectively.

$\overrightarrow{\mathrm{OP}}=\mathbf{a}, \overrightarrow{\mathrm{XQ}}=\mathbf{b}$ and $\overrightarrow{\mathrm{OS}}=\mathbf{c}$.
Show that $P Q$ is parallel to $S R$.

19 The prices of two phones are in the ratio $x: y$.
When the prices are both increased by $£ 20$, the ratio becomes $5: 2$. When the prices are both reduced by $£ 5$, the ratio becomes $5: 1$.

Express the ratio $x: y$ in its lowest terms.

20 (a) Find the interval for which $x^{2}-7 x+10 \leqslant 0$.
(a) ......................... $\leqslant x \leqslant \ldots \ldots \ldots \ldots . . . . . . . . . . . . . . . . .[3]$
[3]
(b) The point $(-3,-4)$ is the turning point of the graph of $y=x^{2}+a x+b$, where $a$ and $b$ are integers.

Find the values of $a$ and $b$.
(b) $a=$ $\qquad$ $b=$

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Date - Morning/Afternoon
GCSE (9-1) Mathematics
J560/05 Paper 5 (Higher Tier)

SAMPLE MARK SCHEME

## MAXIMUM MARK <br> 100



## Subject-Specific Marking Instructions

1. M marks are for using a correct method and are not lost for purely numerical errors.

A marks are for an accurate answer and depend on preceding M (method) marks. Therefore M0 A1 cannot be awarded.
B marks are independent of $\mathbf{M}$ (method) marks and are for a correct final answer, a partially correct answer, or a correct intermediate stage.
SC marks are for special cases that are worthy of some credit.
2. Unless the answer and marks columns of the mark scheme specify $\mathbf{M}$ and $\mathbf{A}$ marks etc, or the mark scheme is 'banded', then if the correct answer is clearly given and is not from wrong working full marks should be awarded.

Do not award the marks if the answer was obtained from an incorrect method, ie incorrect working is seen and the correct answer clearly follows from it.
3. Where follow through (FT) is indicated in the mark scheme, marks can be awarded where the candidate's work follows correctly from a previous answer whether or not it was correct.

Figures or expressions that are being followed through are sometimes encompassed by single quotation marks after the word their for clarity, e.g. FT $180 \times\left(\right.$ their ' 37 ' +16 ), or FT $300-\sqrt{ }\left(\right.$ their ${ }^{\prime} 5^{2}+7^{2}$ ). Answers to part questions which are being followed through are indicated by e.g. FT $3 \times$ their (a).

For questions with FT available you must ensure that you refer back to the relevant previous answer. You may find it easier to mark these questions candidate by candidate rather than question by question.
4. Where dependent (dep) marks are indicated in the mark scheme, you must check that the candidate has met all the criteria specified for the mark to be awarded.
5. The following abbreviations are commonly found in GCSE Mathematics mark schemes.

- figs 237, for example, means any answer with only these digits. You should ignore leading or trailing zeros and any decimal point e.g. $237000,2.37,2.370,0.00237$ would be acceptable but 23070 or 2374 would not.
- isw means ignore subsequent working after correct answer obtained and applies as a default.
- nfww means not from wrong working.
- oe means or equivalent.
- rot means rounded or truncated.
- seen means that you should award the mark if that number/expression is seen anywhere in the answer space, including the answer line, even if it is not in the method leading to the final answer.
- soi means seen or implied.

6. In questions with no final answer line, make no deductions for wrong work after an acceptable answer (ie isw) unless the mark scheme says otherwise, indicated by the instruction 'mark final answer'.
7. In questions with a final answer line following working space:
(i) If the correct answer is seen in the body of working and the answer given on the answer line is a clear transcription error allow full marks unless the mark scheme says 'mark final answer'. Place the annotation $\checkmark$ next to the correct answer.
(ii) If the correct answer is seen in the body of working but the answer line is blank, allow full marks. Place the annotation $\checkmark$ next to the correct answer.
(iii) If the correct answer is seen in the body of working but a completely different answer is seen on the answer line, then accuracy marks for the answer are lost. Method marks could still be awarded. Use the M0, M1, M2 annotations as appropriate and place the annotation $\boldsymbol{x}$ next to the wrong answer.
8. In questions with a final answer line:
(i) If one answer is provided on the answer line, mark the method that leads to that answer.
(ii) If more than one answer is provided on the answer line and there is a single method provided, award method marks only.
(iii) If more than one answer is provided on the answer line and there is more than one method provided, award zero marks for the question unless the candidate has clearly indicated which method is to be marked.
9. In questions with no final answer line:
(i) If a single response is provided, mark as usual.
(ii) If more than one response is provided, award zero marks for the question unless the candidate has clearly indicated which response is to be marked.
10. When the data of a question is consistently misread in such a way as not to alter the nature or difficulty of the question, please follow the candidate's work and allow follow through for $\mathbf{A}$ and $\mathbf{B}$ marks. Deduct 1 mark from any $\mathbf{A}$ or $\mathbf{B}$ marks earned and record this by using the MR annotation. M marks are not deducted for misreads.
11. Unless the question asks for an answer to a specific degree of accuracy, always mark at the greatest number of significant figures even if this is rounded or truncated on the answer line. For example, an answer in the mark scheme is 15.75 , which is seen in the working. The candidate then rounds or truncates this to $15.8,15$ or 16 on the answer line. Allow full marks for the 15.75 .
12. Ranges of answers given in the mark scheme are always inclusive.
13. For methods not provided for in the mark scheme give as far as possible equivalent marks for equivalent work. If in doubt, consult your Team Leader.
14. Anything in the mark scheme which is in square brackets [...] is not required for the mark to be earned, but if present it must be correct.

| Question |  | Answer | Marks | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | (a) | $[p=] 5 \quad[q=]-5$ | $\begin{gathered} \hline 2 \\ 1 \mathrm{AO} 1.2 \\ 1 \mathrm{AO} 1.3 \mathrm{a} \end{gathered}$ | B1 for each |  |
|  | (b) |  | $\begin{gathered} 3 \\ 3 \text { AO1.3a } \end{gathered}$ | B1 for each |  |
| 2 | (a) | 800 | $\begin{gathered} \hline 2 \\ 1 \text { AO1.3b } \\ \text { 1 AO3.1c } \end{gathered}$ | M1 for unitary work, e.g. 1 person does 200 letters in 2 hours |  |
|  | (b) | 30 minutes oe | $\begin{gathered} \hline 4 \\ 2 \mathrm{AOO} .1 \mathrm{a} \\ 2 \mathrm{AO} 3.1 \mathrm{~d} \end{gathered}$ | M1 for 1 person does 100 letters in 1 hour <br> M1 for 5 people do 1000 letters in 2 hours <br> M1 for 4 people do 1000 letters in 2.5 hours <br> FT from their rate in (a) throughout |  |
|  | (c) | Correct comment on the reasonableness of her assumption e.g. 'She has assumed that 'all day' means 'for 24 hours', but it is not reasonable for them to work without a break.' Correct comment on the effect it will have on the answer e.g. 'They can't work at that rate for that long, so her answer is an overestimate.' | $\begin{gathered} \hline 2 \\ 1 \text { AOB.4a } \\ 1 \text { AOO. } \end{gathered}$ | B1 for each |  |
| 3 | (a) | Outcomes not equally likely oe | $\begin{gathered} 1 \\ 1 \text { AO3.4b } \end{gathered}$ |  |  |


| Question |  | Answer | Marks | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | (b) | Larger number of trials | $\begin{gathered} 1 \\ 1 \text { AO3.4a } \end{gathered}$ |  |  |
|  | (c) | 0.09-0.16 | $\begin{gathered} \hline 2 \\ 1 \text { AO1.3a } \\ 1 \mathrm{AOO} .1 \mathrm{~b} \end{gathered}$ | M1 for $\left(\frac{48}{150}\right)^{2}$ or $0.35^{2}$ or any reasonable estimate (FT their (b)) |  |
| 4 | (a) | $\begin{aligned} & 400 \mathrm{~g} \\ & 200 \mathrm{~g} \\ & 300 \mathrm{~g} \end{aligned}$ | $\begin{gathered} 2 \\ \text { 1 AO1.3a } \\ \text { 1 AO3.1c } \end{gathered}$ | M1 for 9 soi |  |
|  | (b) | Profit $=£ 18.20$ |  <br> 5 <br> 2 AO1.3b <br> 2 AO3.1d <br> 1 AO3.3 | M1 Multiply their weights by 5 <br> M1 Find number of each required <br> M1* calculate total cost <br> *M1 dep subtract from $£ 60$ |  |
| 5 |  | $2 a+1$ | 4 1 AO1.3b 2 AO3.1b 1 AO3.2 | M1 for $a+2+3 a+3+4 a-1$ <br> M1 for collecting terms <br> M1 for dividing their ' $8 a+4$ ' by 4 |  |
| 6 |  | $\begin{aligned} & 5 \text { red } \\ & 20 \text { blue } \end{aligned}$ | 3 1 AO1.3b 1 AO3.1b 1 AO3.2 | M1 for listing at least two pairs of red and blue marbles giving a probability $\frac{1}{5}$ <br> M1 for at adding 5 red marbles to at least two pairs <br> SC2 for 10 and 20 pairing seen |  |


| Question |  | Answer | Marks | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 7 |  | $\begin{aligned} & 8 \mathrm{~cm} \\ & 10 \mathrm{~cm} \end{aligned}$ | 3 1 AO1.3a 1 AO3.1b 1 A03.2 | M1 for listing square numbers and finding differences <br> M1 for square rooting their pair of square numbers |  |
| 8 |  | 6 | 3 1 AO1.3b 1 AO3.1d 1 AO3.3 | B1 for 0.75 m <br> M1 for $\frac{4}{\text { their }{ }^{\prime} 0.75 \text { ' }}$ <br> Or $5 \times 0.75=3.75$ |  |
| 9 |  | ```Volume of cuboid = 100000 cm Mass of cuboid = 270 kg Yes, because 270 < 300kg``` | 4 1 AO1.3b 2 AO3.1d 1 AO3.3 | B3 for 270 kg <br> or <br> M1 for $100000 \mathrm{~cm}^{3}$ OR $0.1 \mathrm{~m}^{3}$ OR <br> $100 \mathrm{~cm} \times 50 \mathrm{~cm} \times 20 \mathrm{~cm}$ OR <br> $1 \mathrm{~m} \times 0.5 \mathrm{~m} \times 0.2 \mathrm{~m}$ <br> M1 for $2.7 \times$ their ' 100000 ' OR <br> $2700000 \times$ their ' ${ }^{\prime} .1$ ' |  |
| 10 | (a) | 19 | $\begin{gathered} 1 \\ 1 \text { AO2.3a } \end{gathered}$ |  |  |



| Question |  | Answer | Marks | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | (a) | Both sections of graph correct | $\begin{gathered} 3 \\ 1 \text { AO1.3b } \\ 2 \text { AO2.3b } \end{gathered}$ | B1 for plotting a line segment from the origin to $(4,5)$ <br> B1 for plotting a line segment from their ' $\left(4,5\right.$ )' to their ( 4 ' $+2,{ }^{\prime} 5$ ' -2 ) |  |
|  | (b) | 18 | $\begin{gathered} \hline 3 \\ \text { 2 AA1.3a } \\ \text { 1AO2.3a } \end{gathered}$ | M2 for $\frac{1}{2}(5 \times 4)+\frac{1}{2}(5+3) \times 2$ <br> or <br> M1 for attempt to find area under graph | Accept alt ways to split area <br> FT their graph |
| 12 |  | $\frac{2}{3}$ | 3 1 AO1.3a 1 AO3.1b 1 AO3.2 | B1 for radius of large circle $=3 \times$ radius of small circle <br> M1 for $\frac{9 \pi r^{2}-3\left(\pi r^{2}\right)}{9 \pi r^{2}} \mathbf{o e}$ |  |
| 13 | (a) | 42 | $\begin{gathered} \hline 2 \\ 1 \text { A01.3a } \\ 1 \text { AO2.3a } \end{gathered}$ | M1 for 46 or 4 seen |  |
|  | (b) | World War I in film Smallest range / IQR | $\begin{gathered} 2 \\ 2 \text { AO2.1b } \end{gathered}$ | $\begin{aligned} & \hline \text { M1 } \\ & \text { M1 } \end{aligned}$ |  |




| Question |  | Answer | Marks | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 18 |  | $\begin{aligned} & \overrightarrow{Z Y}=-2 \mathbf{c}+2 \mathbf{a}+2 \mathbf{b} \\ & \overrightarrow{S R}=\mathbf{c}+(-\mathbf{c}+\mathbf{a}+\mathbf{b}) \\ & \text { so } \overrightarrow{S R}=\mathbf{a}+\mathbf{b} \\ & \overrightarrow{P Q}=\mathbf{a}+\mathbf{b} \\ & \overrightarrow{S R}=\overrightarrow{P Q} \text { so they are parallel } \end{aligned}$ | $\begin{gathered} 5 \\ 1 \text { AO1.3a } \\ 2 \text { AOO.2 } \\ 2 \text { AO2.4b } \end{gathered}$ | M1 for $\overrightarrow{Z Y}=-2 c+2 a+2 b$ <br> $\mathbf{M 1}$ for $\overrightarrow{S R}=\mathbf{c}+(-\mathbf{c}+\mathbf{a}+\mathbf{b})$ <br> $\mathbf{M 1}$ for $\overrightarrow{S R}=\mathbf{a}+\mathbf{b}$ <br> $\mathbf{M 1}$ for $\overrightarrow{P Q}=\mathbf{a}+\mathbf{b}$ |  |
| 19 |  | 4:1 | $\begin{gathered} 6 \\ 2 \text { AO1.3b } \\ \text { 4 AO3.1d } \end{gathered}$ | M1 for $(x+20):(y+20)=5: 2$ or $(x-5):(y-5)=5: 1$ <br> A1 for $\frac{x+20}{y+20}=\frac{5}{2}$ oe <br> A1 for $\frac{x-5}{y-5}=\frac{5}{1}$ oe <br> M1 for solving their simultaneous equations <br> A1 for $x=80$ or $y=20$ | Do not accept wrong notation for ratio in the final mark, e.g. for $4 / 1,4$, etc |
| 20 | (a) | $2 \leq x \leq 5$ | $\begin{gathered} 3 \\ 3 \text { AO1.3b } \end{gathered}$ | M1 for factorising $(x-5)(x-2)$ soi <br> A1 for 2 and 5 | Answer may be on a number line in which case the ends must be clearly seen |
|  | (b) | $[a=] 6 \quad[b=] 5$ | 1 <br> 1 AO1.3b <br> 1 AO2.1a <br> 1 AO3.1b | M1 for $y=(x+3)^{2}-4$ <br> M1 for multiplying out and simplifying their $y=(x+3)^{2}-4$ |  |

Assessment Objectives (AO) Grid

| Question | A01 | AO2 | AO3 | Total |
| :---: | :---: | :---: | :---: | :---: |
| 1(a) | 2 |  |  | 2 |
| 1(b) | 3 |  |  | 3 |
| 2(a) | 1 |  | 1 | 2 |
| 2(b) |  | 2 | 2 | 4 |
| 2(c) |  |  | 2 | 2 |
| 3(a) |  |  | 1 | 1 |
| 3(b) |  |  | 1 | 1 |
| 3(c) | 1 | 1 |  | 2 |
| 4(a) | 1 |  | 1 | 2 |
| 4(b) | 2 |  | 3 | 5 |
| 5 | 1 |  | 3 | 4 |
| 6 | 1 |  | 2 | 3 |
| 7 | 1 |  | 2 | 3 |
| 8 | 1 |  | 2 | 3 |
| 9 | 1 |  | 3 | 4 |
| 10(a) |  | 1 |  | 1 |
| 10(b) |  | 1 |  | 1 |
| 10(c) |  | 2 |  | 2 |
| 10(d) | 2 | 2 |  | 4 |
| 11(a) | 1 | 2 |  | 3 |
| 11(b) | 2 | 1 |  | 3 |
| 12 | 1 |  | 2 | 3 |
| 13(a) | 1 | 1 |  | 2 |
| 13(b) |  | 2 |  | 2 |
| 13(c) |  | 2 |  | 2 |
| 13(d) |  | 2 |  | 2 |
| 14 | 1 | 3 |  | 4 |
| 15(a) | 2 |  |  | 2 |
| 15(b) | 3 |  |  | 3 |
| 16 |  | 3 |  | 3 |
| 17(a) | 1 |  |  | 1 |
| 17(b) | 4 |  |  | 4 |
| 18 | 1 | 4 |  | 5 |
| 19 | 2 |  | 4 | 6 |
| 20(a) | 3 |  |  | 3 |
| 20(b) | 1 | 1 | 1 | 3 |
| Totals | 40 | 30 | 30 | 100 |

Oxford Cambridge and RSA

## GCSE (9-1) Mathematics J560/06 Paper 6 (Higher Tier) Sample Question Paper

## Date - Morning/Afternoon

Time allowed: 1 hour 30 minutes

## You may use:

- A scientific or graphical calculator
- Geometrical instruments
- Tracing paper



## INSTRUCTIONS

- Use black ink. You may use an HB pencil for graphs and diagrams.
- Complete the boxes above with your name, centre number and candidate number.
- Answer all the questions.
- Read each question carefully before you start to write your answer.
- Where appropriate, your answers should be supported with working. Marks may be given for a correct method even if the answer is incorrect.
- Write your answer to each question in the space provided.
- Additional paper may be used if required but you must clearly show your candidate number, centre number and question number(s).
- Do not write in the bar codes.


## INFORMATION

- The total mark for this paper is 100.
- The marks for each question are shown in brackets [ ].
- Use the $\pi$ button on your calculator or take $\pi$ to be 3.142 unless the question says otherwise.
- This document consists of 20 pages.


## Answer all the questions

1180 g of copper is mixed with 105 g of zinc to make an alloy.
The density of copper is $9 \mathrm{~g} / \mathrm{cm}^{3}$.
The density of zinc is $7 \mathrm{~g} / \mathrm{cm}^{3}$.
(a) Work out the volume of copper used in the alloy.
(a) $\qquad$ $\mathrm{cm}^{3}$ [2]
(b) What is the density of the alloy?
(b)
$\mathrm{g} / \mathrm{cm}^{3}$ [4]

2 (a) (i) Solve.

$$
5 x+1>x+13
$$

(a)(i)
(ii) Write down the largest integer that satisfies $5 x-1<10$.

> (ii)
(b) Solve.

$$
3 x^{2}=75
$$

(b) $x=$
(c) Solve.

$$
\begin{aligned}
& 4 x+3 y=5 \\
& 2 x+3 y=1
\end{aligned}
$$

(c) $x=$

$$
y=
$$

3 (a) This expression can be used to generate a sequence of numbers.

$$
n^{2}-n+11
$$

(i) Work out the first three terms of this sequence.
(a)(i)
(ii) Show that this expression does not only generate prime numbers.
$\qquad$
(b) Marta says
odd square numbers have exactly three factors.
Give one example where this is correct and another where this is not correct. In each case, write down the number and its factors.

Correct $\qquad$
Not correct $\qquad$
(c) Here are some properties of a number.

- It is a common factor of 288 and 360.
- It is a common multiple of 4 and 6.
- It is larger than 25.

Find the two possible numbers with these properties.
(c) $\qquad$ and

4 Here are the interest rates for two accounts.

| Account A |
| :--- |
| Interest: |
| 3\% per year compound |
| interest. |
| No withdrawals until the <br> end of three years. |

## Account B

Interest:
4\% for the first year,
$3 \%$ for the second year
and
$2 \%$ for the third year.
Withdrawals allowed at any time.

Derrick has $£ 10000$ he wants to invest.
(a) Calculate which account would give him most money if he invests his money for 3 years. Give the difference in the interest to the nearest penny.
(a) Account $\qquad$ by $\qquad$
(b) Explain why he might not want to use Account A.
$\qquad$

5 Lei is in a class of 28 students, 3 of whom are left-handed. There are 1250 students in the school.
(a) Use this information to estimate how many students in the school are left-handed.
(a)
(b) Is your solution to (a) likely to be an overestimate or an underestimate? Explain your reasoning.
$\qquad$
(c) Vid is at a different school.

He is in a class of 26 students, 6 of whom are left-handed.

Vid says to Lei

In our two classes there are 54 students, 9 of whom are left-handed.
We can use this bigger sample to improve the estimate for your school.
What assumption has Vid made?
Explain whether you think that his argument is correct.
$\qquad$
$\qquad$

6 John wants to investigate whether men in the UK are better at estimating a time interval of 10 seconds than women in the UK. He decides to sample the population by asking his work colleagues to take the test.

The diagrams below summarise John's results.



(a) What information from the diagrams can be used to support each of these statements?
(i) The older John's colleagues are, the lower their estimate is.
$\qquad$
$\qquad$
(ii) Males in the sample tend to underestimate the interval and females in the sample tend to overestimate the interval.
$\qquad$
(b) Comment on whether any conclusions can be drawn for the UK population from the results of this sample.
$\qquad$

7 Without using a calculator, show clearly that $64^{\frac{2}{3}}$ is equal to 16 .

8 (a) Prove that the sum of four consecutive whole numbers is always even.
(b) Give an example to show that the sum of four consecutive integers is not always divisible by 4 .

9 Alexander, Reiner and Wim each watch a different film.

- Alexander's film is thirty minutes longer than Wim's film.
- Reiner's film is twice as long as Wim's film.
- Altogether the films last 390 minutes.

How long is each of their films?

Alexander's film
minutes

Reiner's film
minutes
Wim's film
minutes

10 The graph shows the distance travelled by an animal over 12 seconds.

(a) Work out the average speed between 2 and 8 seconds.
$\qquad$
(a)
$\mathrm{m} / \mathrm{s}$ [2]
(b) Estimate the speed of the animal at 6 seconds.
(b)
(c) Nuri says

## I think this animal must be able to move at over $20 \mathrm{~m} / \mathrm{s}$ !

Do you agree with Nuri?
Explain your decision.
$\qquad$
$\qquad$

11 A skills test has two sections, literacy (L) and numeracy (N).
One day everyone who took the skills test passed at least one section.
$88 \%$ passed the literacy section and $76 \%$ passed the numeracy section.
(a) Represent this information on a Venn diagram.

Show clearly the percentage in each section of the diagram.

(b) One person is chosen at random from all the people who took the skills test that day.

What is the probability that this person
(i) passed the numeracy section, given that they passed the literacy section,
(b)(i)
(ii) passed the literacy section, given that they passed only one section?
(ii)

12 Two similar pyramids $A$ and $B$ have surface areas $180 \mathrm{~cm}^{2}$ and $80 \mathrm{~cm}^{2}$ respectively.


Pyramid A


Pyramid B

The volume of pyramid A is $810 \mathrm{~cm}^{3}$.
Show that the volume of pyramid B is $240 \mathrm{~cm}^{3}$.

13 Calculate $x$.


Not to scale

14 A straight line goes through the points $(p, q)$ and $(r, s)$, where

- $p+2=r$
- $q+4=s$.

Find the gradient of the line.

15 A unit fraction has a numerator equal to 1 , for example $\frac{1}{3}, \frac{1}{7}$ and $\frac{1}{25}$.
Unit fractions can be written as the sum of two different unit fractions, for example

$$
\frac{1}{2}=\frac{1}{3}+\frac{1}{6}
$$

Write each of the following unit fractions as the sum of two different unit fractions.


16 Simon cuts the corners off a square piece of card to leave the regular octagon shown below. O is the centre of the octagon.
$A$ and $B$ are vertices of the octagon.
$O A=O B=5 \mathrm{~cm}$.
Angle $\mathrm{AOB}=45^{\circ}$.


Not to scale
(a) (i) Work out the area of the octagon.
(ii) Work out the area of the original square piece of card.
(ii)
$\mathrm{cm}^{2}$ [5]
(b) Simon now makes a table top using the card as a model.

The sides of the table top are 8 times as long as the sides of the card model.
Find the ratio of the area of Simon's table top to the area of the card model.
(b)
:
[2]
$y=6 x^{4}+7 x^{2}$ and $x=\sqrt{w+1}$.
Find the value of $w$ when $y=10$.
Show your working.

[^1]Date - Morning/Afternoon
GCSE (9-1) Mathematics
J560/06 Paper 6 (Higher Tier)

SAMPLE MARK SCHEME

MAXIMUM MARK 100

## DRAFT

## Subject-Specific Marking Instructions

1. M marks are for using a correct method and are not lost for purely numerical errors.

A marks are for an accurate answer and depend on preceding M (method) marks. Therefore M0 A1 cannot be awarded.
B marks are independent of $\mathbf{M}$ (method) marks and are for a correct final answer, a partially correct answer, or a correct intermediate stage.
SC marks are for special cases that are worthy of some credit.
2. Unless the answer and marks columns of the mark scheme specify $\mathbf{M}$ and $\mathbf{A}$ marks etc, or the mark scheme is 'banded', then if the correct answer is clearly given and is not from wrong working full marks should be awarded.

Do not award the marks if the answer was obtained from an incorrect method, ie incorrect working is seen and the correct answer clearly follows from it.
3. Where follow through (FT) is indicated in the mark scheme, marks can be awarded where the candidate's work follows correctly from a previous answer whether or not it was correct.

Figures or expressions that are being followed through are sometimes encompassed by single quotation marks after the word their for clarity, e.g. FT $180 \times\left(\right.$ their ' 37 ' +16 ), or FT $300-\sqrt{ }\left(\right.$ their ${ }^{\prime} 5^{2}+7^{2}$ ). Answers to part questions which are being followed through are indicated by e.g. FT $3 \times$ their (a).

For questions with FT available you must ensure that you refer back to the relevant previous answer. You may find it easier to mark these questions candidate by candidate rather than question by question.
4. Where dependent (dep) marks are indicated in the mark scheme, you must check that the candidate has met all the criteria specified for the mark to be awarded.
5. The following abbreviations are commonly found in GCSE Mathematics mark schemes.

- figs 237, for example, means any answer with only these digits. You should ignore leading or trailing zeros and any decimal point e.g. $237000,2.37,2.370,0.00237$ would be acceptable but 23070 or 2374 would not.
- isw means ignore subsequent working after correct answer obtained and applies as a default.
- nfww means not from wrong working.
- oe means or equivalent.
- rot means rounded or truncated.
- seen means that you should award the mark if that number/expression is seen anywhere in the answer space, including the answer line, even if it is not in the method leading to the final answer.
- soi means seen or implied.

6. In questions with no final answer line, make no deductions for wrong work after an acceptable answer (ie isw) unless the mark scheme says otherwise, indicated by the instruction 'mark final answer'.
7. In questions with a final answer line following working space:
(i) If the correct answer is seen in the body of working and the answer given on the answer line is a clear transcription error allow full marks unless the mark scheme says 'mark final answer'. Place the annotation $\checkmark$ next to the correct answer.
(ii) If the correct answer is seen in the body of working but the answer line is blank, allow full marks. Place the annotation $\checkmark$ next to the correct answer.
(iii) If the correct answer is seen in the body of working but a completely different answer is seen on the answer line, then accuracy marks for the answer are lost. Method marks could still be awarded. Use the M0, M1, M2 annotations as appropriate and place the annotation $x$ next to the wrong answer.
8. In questions with a final answer line:
(i) If one answer is provided on the answer line, mark the method that leads to that answer.
(ii) If more than one answer is provided on the answer line and there is a single method provided, award method marks only.
(iii) If more than one answer is provided on the answer line and there is more than one method provided, award zero marks for the question unless the candidate has clearly indicated which method is to be marked.
9. In questions with no final answer line:
(i) If a single response is provided, mark as usual.
(ii) If more than one response is provided, award zero marks for the question unless the candidate has clearly indicated which response is to be marked.
10. When the data of a question is consistently misread in such a way as not to alter the nature or difficulty of the question, please follow the candidate's work and allow follow through for $\mathbf{A}$ and $\mathbf{B}$ marks. Deduct 1 mark from any $\mathbf{A}$ or $\mathbf{B}$ marks earned and record this by using the MR annotation. M marks are not deducted for misreads.
11. Unless the question asks for an answer to a specific degree of accuracy, always mark at the greatest number of significant figures even if this is rounded or truncated on the answer line. For example, an answer in the mark scheme is 15.75 , which is seen in the working. The candidate then rounds or truncates this to $15.8,15$ or 16 on the answer line. Allow full marks for the 15.75 .
12. Ranges of answers given in the mark scheme are always inclusive.
13. For methods not provided for in the mark scheme give as far as possible equivalent marks for equivalent work. If in doubt, consult your Team Leader.
14. Anything in the mark scheme which is in square brackets [...] is not required for the mark to be earned, but if present it must be correct.

| Question |  |  | Answer | Marks | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | (a) |  | 20 | $\begin{gathered} \hline 2 \\ 1 \text { AO1.1 } \\ 1 \text { A02.3a } \end{gathered}$ | M1 for $D=\frac{M}{V}$ soi | Can be implied by an answer of 2 |
|  | (b) |  | $8 \frac{1}{7}$ or $8.14[\ldots]$ | $\begin{gathered} 4 \\ \begin{array}{c} \text { 2AO1.3b } \\ 2 \text { AOB3.1d } \end{array} \end{gathered}$ | M1 for 15 or $105 \div 7$ <br> And <br> M2 for $\frac{180+105}{\text { their }(20+15)}$ or $\frac{18+10.5}{\text { their }(2+1.5)^{\prime}}$ <br> Or <br> M1 for some attempt to find total mass <br> total volume |  |
| 2 | (a) | (i) | $x>3$ | $\begin{gathered} 3 \\ 3 \mathrm{AO1} .3 \mathrm{a} \end{gathered}$ | M1 for $4 x$ soi M1 for 12 soi |  |
|  |  | (ii) | 2 | $\begin{gathered} 1 \\ 1 \text { A01.3a } \end{gathered}$ |  |  |
|  | (b) |  | $\begin{array}{cc}{[+] 5} & -5\end{array}$ | $\begin{gathered} 2 \\ 2 \text { AO1.3a } \end{gathered}$ | M1 for $x^{2}=25$ <br> If zero scored SC1 for 5 seen as answer |  |
|  | (c) |  | $[x=] 2 \quad[y=]-1$ | $\begin{gathered} 3 \\ 3 \text { A01.3b } \end{gathered}$ | M1 for eliminating one variable M1 for correct substitution of their $x$ or y |  |
| 3 | (a) | (i) | 111317 | $\begin{gathered} 2 \\ 2 \mathrm{AO} 1.3 \mathrm{a} \end{gathered}$ | B1 for any two correct |  |


| Question |  |  | Answer | Marks | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | (ii) | Any multiple of 11 and its result e.g. 11 th term is $121=11^{2}$ | $\begin{gathered} 2 \\ \text { 1A01.3a } \\ \text { 1A02.4a } \end{gathered}$ | Accept any correct argument <br> B1 at least two more evaluated terms |  |
|  | (b) |  | [Correct] e.g. $9=(1,3,9)$ or $25=(1,5,25)$ or $49=(1,7,49)$ <br> [ Not correct] e.g. $1=(1)$ or $81=(1,3,9,27$, 81) | $\begin{gathered} 2 \\ 2 \text { AO2.4a } \end{gathered}$ | B1 for each | Factors given must be correct for each number given for B1 |
|  | (c) |  | 36 and 72 | $\begin{gathered} 4 \\ \text { 2 AO1.3a } \\ \text { 2 AOB3.1b } \end{gathered}$ | B1 for common factors of 288 and 360 found, e.g. 2, 3, 6, 8, 9, 12, 18, 24, 36, 72 <br> and <br> B1 for common multiples of 4 and 6 found, e.g. 12, 24, 36, 48, 60, 72, 84, 96 <br> and <br> B1 for 36 or 72 |  |
| 4 | (a) |  | (Account) A (by) 103[p] | 5 <br> 3 AO1.3b <br> 1 AO3.1d <br> 1 AOB.3 | B2 for 10927.27 <br> and <br> B2 for 10926.24 or B1 for 10400 or 10712 <br> If zero scored <br> M1 for $1.03^{3}$ oe used <br> M1 for 1.04, 1.03 and 1.02 used oe |  |
|  | (b) |  | He may not want to leave it there for 3 years | $\begin{gathered} 1 \\ 1 \text { AO2.3a } \end{gathered}$ | Accept any valid reason |  |


| Question |  |  | Answer | Marks | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5 | (a) |  | 120 to 180 | $\begin{gathered} 3 \\ 1 \text { AO1.3a } \\ 1 \text { AO2.1b } \\ 1 \text { AO3.1c } \end{gathered}$ | M1 for proportion of left-handed between $\frac{1}{7}$ and $\frac{1}{10}$ <br> M1 for their '1250' $\times$ their proportion |  |
|  | (b) |  | Correct explanation for their answer, e.g. 'underestimate because I rounded to 3 out of 30 oe or "overestimate because I rounded to 4 out of 28 ' oe <br> or 'Not possible to tell because we only have a small sample' oe | $\begin{gathered} 1 \\ 1 \text { AO3.4b } \end{gathered}$ | FT from their (a) |  |
|  | (c) |  | 'He has assumed that the populations of the two schools have approximately the same proportion of left-handers.' oe <br> Correct explanation for their decision, 'Yes. This is a bigger sample so it should give a more reliable estimate.' oe or <br> 'No. The two samples are from different populations, so we can't use Vid's class to infer properties of Lei's school.' oe | $\begin{gathered} \hline 2 \\ 1 \text { AO2.5a } \\ 1 \text { AOO.5 } \end{gathered}$ | B1 for identification of assumption B1 for correct explanation for their decision |  |
| 6 | (a) | (i) | [Using the scatter diagram] the points slope down/negative correlation | $\begin{gathered} 1 \\ 1 \text { AO2.1a } \end{gathered}$ |  |  |
|  |  | (ii) | [Using diagrams 1 and 2] 15/24 males have less than 10 so more than half underestimate, 10/16 females have more than 10 so more than half over-estimate | $\begin{gathered} 2 \\ 2 \text { AO2.1a } \end{gathered}$ | B1 for 15/24 males estimate less than 10 seconds <br> B1 for 10/16 females estimate more than 10 seconds |  |


| Question |  | Answer | Marks | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | (b) | No; it is a very small sample, so it doesn't represent the population very well | $\begin{gathered} 2 \\ 1 \mathrm{AOO} .1 \mathrm{a} \\ 1 \mathrm{AOB} .4 \mathrm{a} \end{gathered}$ | B1 for any relevant comment, e.g. small sample, more men than women, John's work may involve estimating time so the sample is biased, etc. <br> B1 for "No" |  |
| 7 |  | $\begin{aligned} & \left(64^{\frac{1}{3}}\right)^{2} \\ & =4^{2}=16 \end{aligned}$ | $\begin{gathered} 2 \\ 2 \mathrm{AOO} .2 \end{gathered}$ | B1 for (64 $\left.{ }^{\frac{1}{3}}\right)^{2}, 4^{2}$ or $\sqrt[3]{4096}$ oe | Condone $\left(64^{2}\right)^{\frac{1}{3}}$ and $(4096)^{\frac{1}{3}}$ for B1 |
| 8 | (a) | $\begin{aligned} & x, x+1, x+2, x+3 \\ & x+(x+1)+(x+2)+(x+3) \text { or } 4 x+6 \\ & 2(x+3) \end{aligned}$ | $\begin{gathered} 1 \\ 1 \\ 1 \\ \text { 3 AO2.4b } \end{gathered}$ | accept correct alternatives |  |
|  | (b) | $\begin{aligned} & \text { e.g. } 1+2+3+4 \\ & 4 x+6 \text { is not a multiple of } 4 \end{aligned}$ |  | Allow e.g. $1+2+3+4=10$ is not a multiple of 4 |  |
| 9 |  | ```Alexander = 120 (minutes) Reiner = 180 (minutes) Wim = 90 (minutes)``` | 4 <br> 2 AO1.3b <br> 1 AO3.1d <br> 1 AO3.3 | M1 for any two correct expressions, e.g $r=2 w, a=w+30, a+r+w=390$ M1 for equating one variable, e.g. $w+$ $30+2 w+w=390$ oe <br> A1 for solving for one variable, e.g. $w$ = 90 oe |  |
| 10 | (a) | 7.1 to 7.2 | $\begin{gathered} 2 \\ 2 \text { A01.3b } \end{gathered}$ | M1 for $(47-4) \div(8-2)$, allow one error |  |


| Question |  |  | Answer | Marks | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | (b) |  | 7.5 to 8.5 | 4 1 AO1.3a 2 AO2.1b 1 AO2.3a | M1 for an attempt to draw a tangent drawn at 6 <br> and <br> M2 for their distance $\div$ their time e.g. $(40-2) \div(8-3)$ with a time gap of at least two seconds or <br> M1 for an inaccurate attempt at distance $\div$ time (FT their tangent) | Accuracy $\pm 1 \mathrm{~mm}$ |
|  | (c) |  | Agreement, with correct reasoning | $\begin{gathered} 2 \\ 1 \text { AO2.3a } \\ 1 \text { AO3.4b } \end{gathered}$ | B1 for agreement, with partial reasoning |  |
| 11 | (a) |  |  | $\begin{gathered} \hline 3 \\ 1 \text { AO2.3a } \\ 2 \mathrm{AOO} .3 \mathrm{~b} \end{gathered}$ $2 \text { AO2.3b }$ | B1 for 24\% in L and <br> B1 for $12 \%$ in N and M1 for 100 - (their ' 12 ' + their ' 24 ') in overlap | Condone universal set missing |
|  | (b) | (i) | $\frac{64}{88} \text { oe }$ | $\begin{gathered} 2 \\ 2 \text { AO1.3a } \end{gathered}$ | M1 for 64 or 88 | FT their Venn diagram |
|  |  | (ii) | $\frac{24}{36}$ oe | $\begin{gathered} 2 \\ 2 \mathrm{AO} 1.3 \mathrm{a} \end{gathered}$ | M1 for 24 or 36 | FT their Venn diagram |



| Question |  |  | Answer | Marks | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 15 |  |  | Correct solutions, e.g. $\begin{aligned} & \frac{1}{4}=\frac{1}{6}+\frac{1}{12} \\ & \frac{1}{5}=\frac{1}{6}+\frac{1}{30} \\ & \frac{1}{6}=\frac{1}{9}+\frac{1}{18} \end{aligned}$ | $\begin{gathered} 3 \\ 1 \text { AOO.1. } \\ \text { 2 AOB.1a } \end{gathered}$ | B1 for each <br> Allow any correct example, e.g. $\begin{aligned} & \frac{1}{4}=\frac{1}{5}+\frac{1}{20} \\ & \frac{1}{6}=\frac{1}{7}+\frac{1}{42} \end{aligned}$ |  |
| 16 | (a) | (i) | 70.71[0678...] | $\begin{gathered} 3 \\ 1 \text { AOO1.1 } \\ \text { 2 AO3.1a } \end{gathered}$ | M2 for $8 \times \frac{1}{2} \times 5 \times 5 \times \sin 45$ or M1 for $\frac{1}{2} \times 5 \times 5 \times \sin 45$ |  |
|  |  | (ii) | 85-85.4 | $\begin{gathered} 5 \\ 2 \text { A AO1.3b } \\ 3 \text { AOB.1b } \end{gathered}$ | M4 for $(2 \times 5 \cos 22.5)^{2} \text { or }(2 \times 5 \sin 67.5)^{2}$ <br> or <br> M3 for $2 \times 5 \cos 22.5$ or $2 \times 5 \sin 67.5$ or <br> M2 for $5 \cos 22.5$ or $5 \sin 67.5$ or <br> M1 for $\cos 22.5=\frac{x}{5}$ or $\sin 67.5=\frac{x}{5}$ | 9.238... <br> 4.619... |
|  | (b) |  | $64: 1$ or $1: \frac{1}{64}$ | $\begin{gathered} 2 \\ 2 \text { AO3.2 } \end{gathered}$ | M1 for making the link to, and using, enlargement eg $\left(\frac{1}{8}\right)^{2}$ or $8^{2}$ soi |  |



Assessment Objectives (AO) Grid

| Question | A01 | AO2 | AO3 | Total |
| :---: | :---: | :---: | :---: | :---: |
| 1(a) | 1 | 1 |  | 2 |
| 1(b) | 2 |  | 2 | 4 |
| 2(a)(i) | 3 |  |  | 3 |
| 2(a)(ii) | 1 |  |  | 1 |
| 2(b) | 2 |  |  | 2 |
| 2(c) | 3 |  |  | 3 |
| 3(a)(i) | 2 |  |  | 2 |
| 3(a)(ii) | 1 | 1 |  | 2 |
| 3(b) |  | 2 |  | 2 |
| 3(c) | 2 |  | 2 | 4 |
| 4(a) | 3 |  | 2 | 5 |
| 4(b) |  | 1 |  | 1 |
| 5(a) | 1 | 1 | 1 | 3 |
| 5(b) |  |  | 1 | 1 |
| 5(c) |  | 1 | 1 | 2 |
| 6(a)(i) |  | 1 |  | 1 |
| 6(a)(ii) |  | 2 |  | 2 |
| 6(b) |  | 1 | 1 | 2 |
| 7 |  | 2 |  | 2 |
| 8(a) |  | 3 |  | 3 |
| 8(b) |  | 2 |  | 2 |
| 9 | 2 |  | 2 | 4 |
| 10(a) | 2 |  |  | 2 |
| 10(b) | 1 | 3 |  | 4 |
| 10(c) |  | 1 | 1 | 2 |
| 11(a) |  | 3 |  | 3 |
| 11(b)(i) | 2 |  |  | 2 |
| 11(b)(ii) | 2 |  |  | 2 |
| 12 | 1 | 4 |  | 5 |
| 13 | 3 |  | 2 | 5 |
| 14 | 1 |  | 2 | 3 |
| 15 | 1 |  | 2 | 3 |
| 16(a)(i) | 1 |  | 2 | 3 |
| 16(a)(ii) | 2 |  | 3 | 5 |
| 16(b) |  |  | 2 | 2 |
| 17 | 1 | 1 | 4 | 6 |
| Totals | 40 | 30 | 30 | 100 |


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